

INTERFEROMETRY & EXOPLANETS

PLATO STESCI Workshop
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ROXANNE LIGI

INAF-Osservatorio Astronomico di Brera
Marie Skłodowska-Curie/AstroFlt2 Fellow

In collaboration with:

Ennio Poretti (INAF-OA Brera) · Francesco Borsa (INAF-OA Brera) · Monica Rainer (INAF-OA Brera) · Denis Mourard (OCA) · Nicolas Nardetto (OCA) · Lionel Bigot (OCA) · Andrea Chiavassa (OCA) · Oragh Creevey (OCA) · Aurélien Crida (OCA) · Caroline Dorn (Univ. Zurich) · Yveline Lebreton (Univ. Rennes/OBSPM) · VEGA/CHARA team

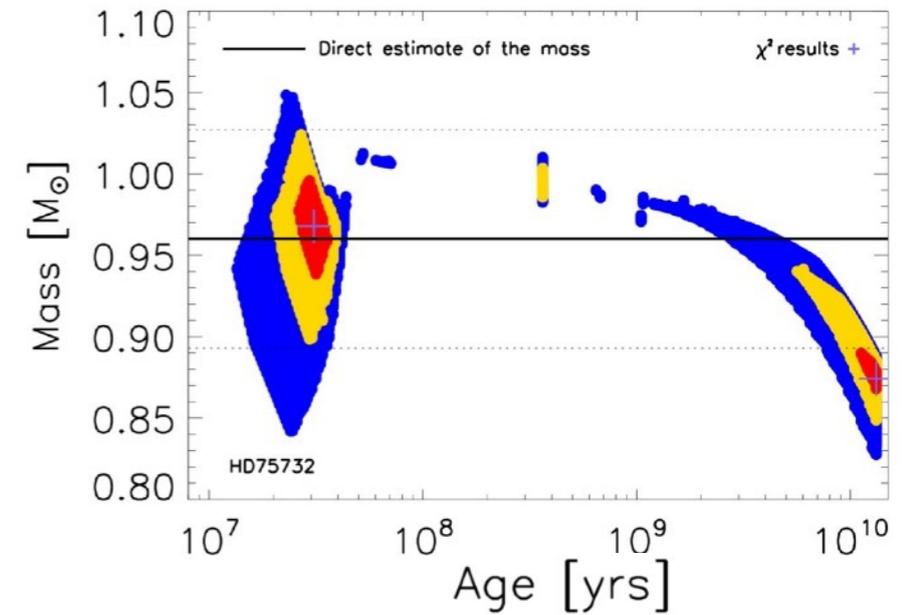
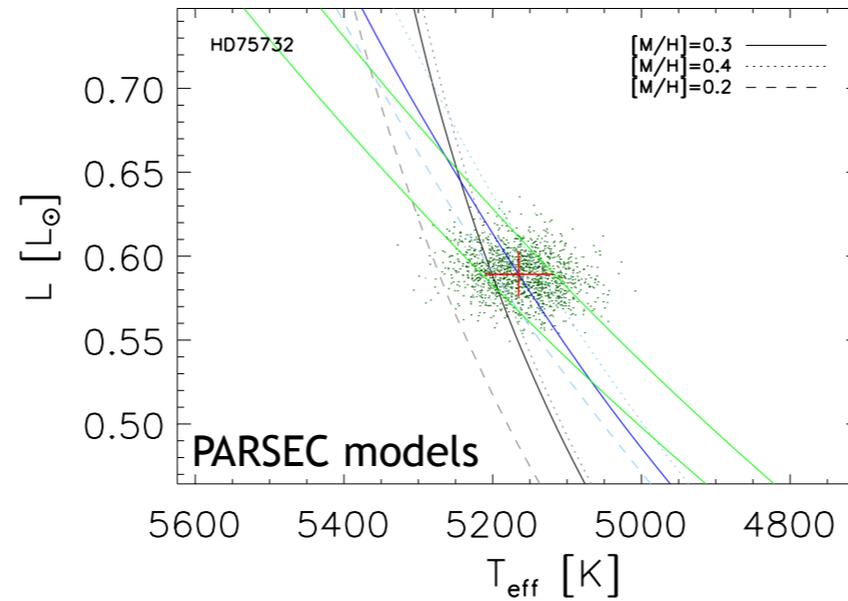
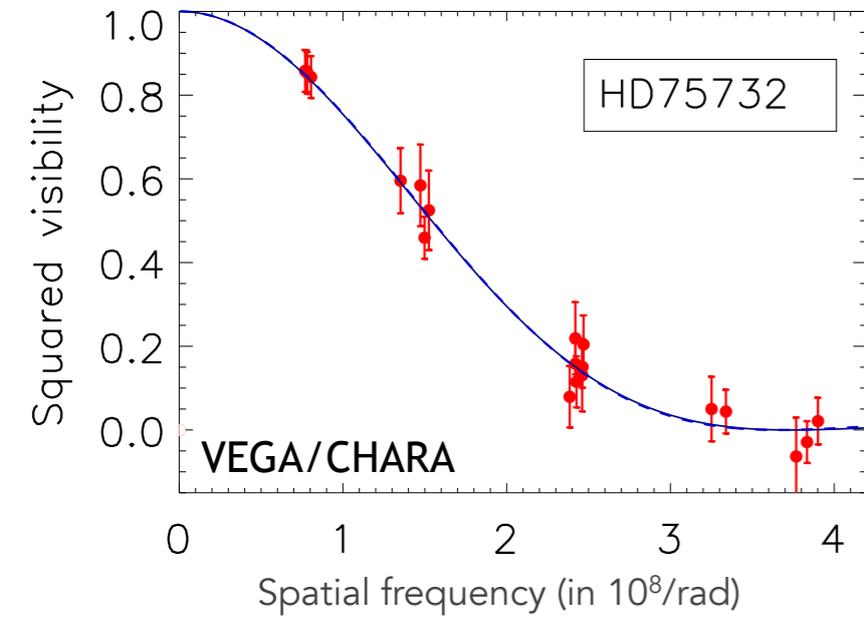
55 CNC AND ITS TRANSITING EXOPLANET

A habitable planet around 55 Cancri?

- 55 Cnc: 5 exoplanets
- 55 Cnc e transits its star, and is a super-Earth (*Winn et al. 2011, Demory et al. 2011*)
- Well studied stars



55 CNC AND ITS TRANSITING EXOPLANET



- From isochrones: 2 solutions
 - **Young solution:** $M_{\star} = 0.968 \pm 0.018 M_{\odot}$, 30.0 ± 3.028 Myrs
 - **Old solution:** $M_{\star} = 0.874 \pm 0.013 M_{\odot}$, 13.19 ± 1.18 Gyrs

55 CNC AND ITS TRANSITING EXOPLANET

Transit duration: $T = 2R_{\star}/a\Omega$

Period: $P = 2\pi/\Omega$

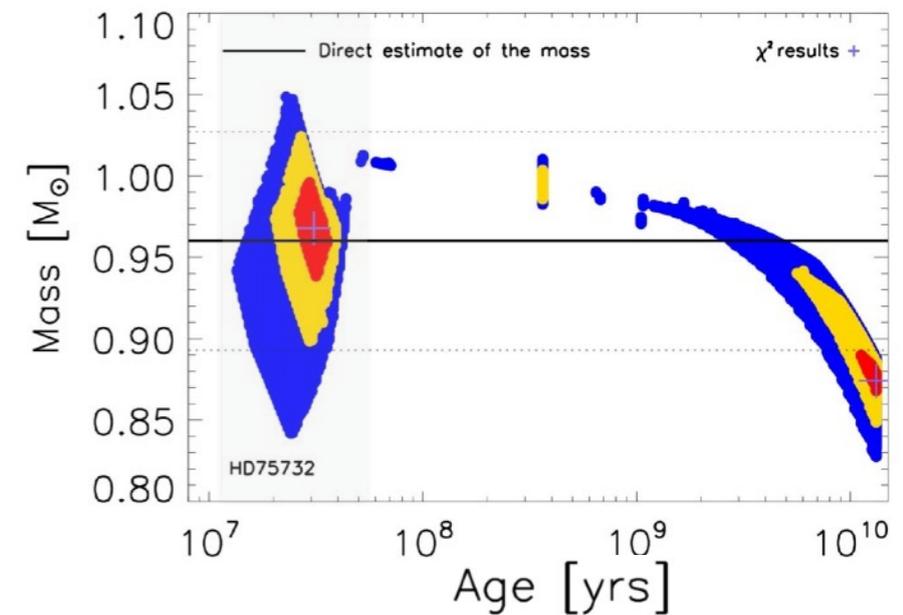
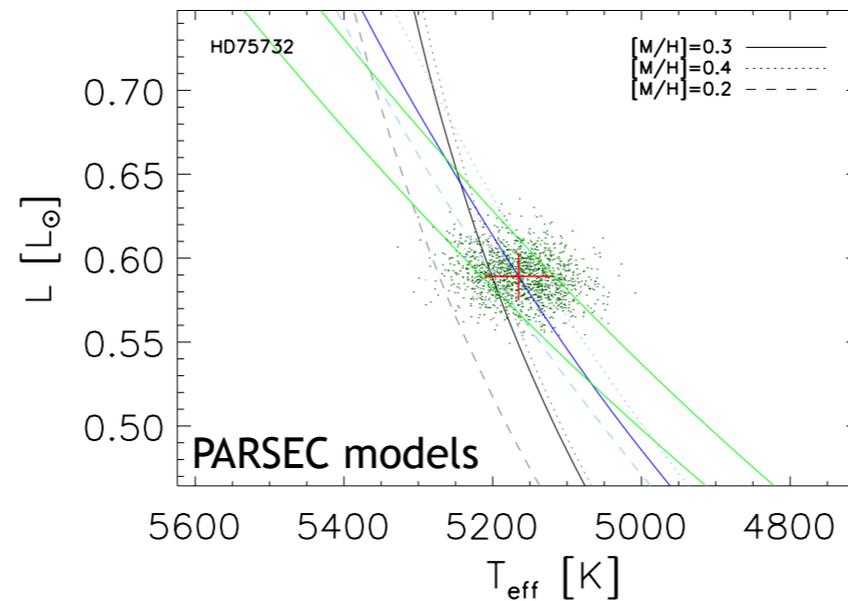
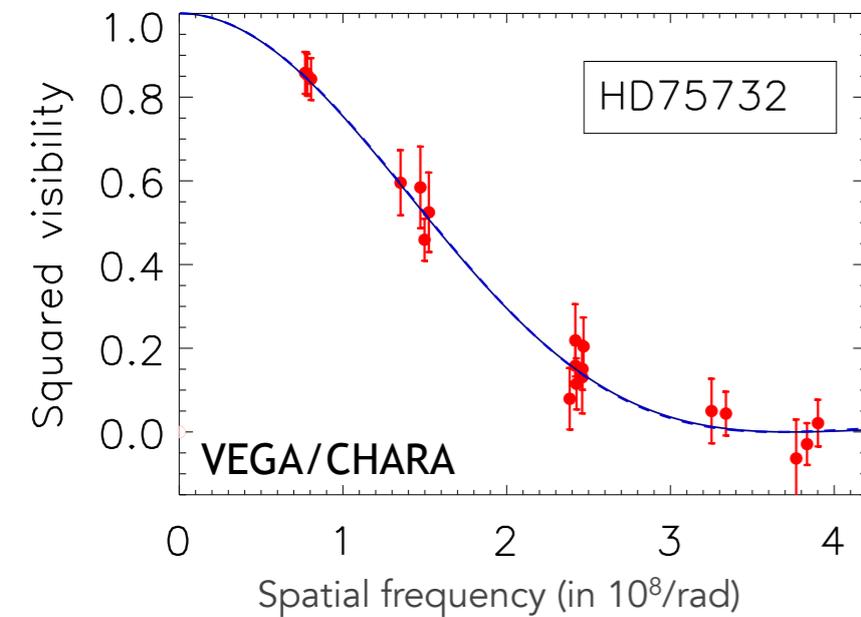


$$P/T^3 = (\pi^2 G/3) \rho_{\star}$$

measure of stellar density ρ_{\star} (Maxted et al. 2015, Seager & Mallén-Ornelas 2003)

Measure of R_{\star} by interferometry $\rightarrow M_{\star} = (4\pi/3)R_{\star}^3 \rho_{\star}$ (Ligi et al. 2016)

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 - **Old solution:** $M_{\star} = 0.874 \pm 0.013 M_{\odot}$, 13.19 ± 1.18 Gyrs
- Using the stellar density + interferometric radius: $M_{\star} = 0.96 \pm 0.067 M_{\odot}$

55 CNC: A BAYESIAN APPROACH

Observations: θ , π (parallax), $m \rightarrow F_{\text{bol}}$, the bolometric flux.

Crida, Ligi, Dorn & Lebreton, arXiv:1804.07537.

Crida & Ligi, EPSC 2017

$$L = 4 F_{\text{bol}} (1_{[\text{pc}]} / \pi)^2$$

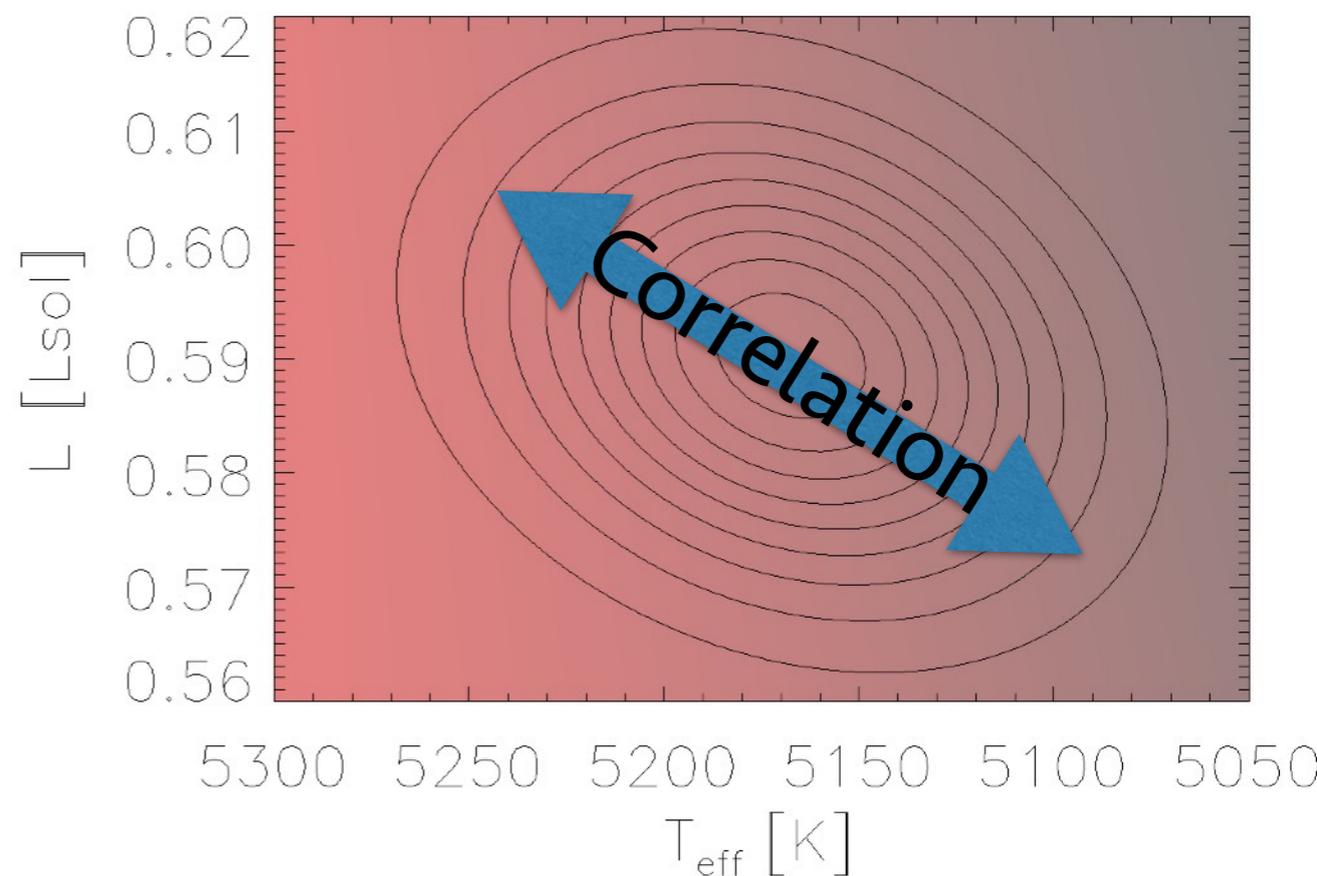
$$T_{\text{eff}} = (4 F_{\text{bol}} / \sigma_{\text{SB}} \theta)^{1/4}$$

Likelihood
(analytic)

$$\mathcal{L}_{\text{HR}}(L, T) = \frac{4\sqrt{\pi/\sigma_{\text{SB}}}}{L^{3/2}T^3} \times \int_0^{+\infty} t \times f_{F_{\text{bol}}}(t) \times f_{\Pi} \left(\sqrt{\frac{4\pi t}{L}} \right) \times f_{\theta} \left(\sqrt{\frac{4t}{\sigma_{\text{SB}} T^4}} \right) dt. \quad (3)$$

Prior: density of stars in the HR diagram of the Hipparcos sample (color).

level curves



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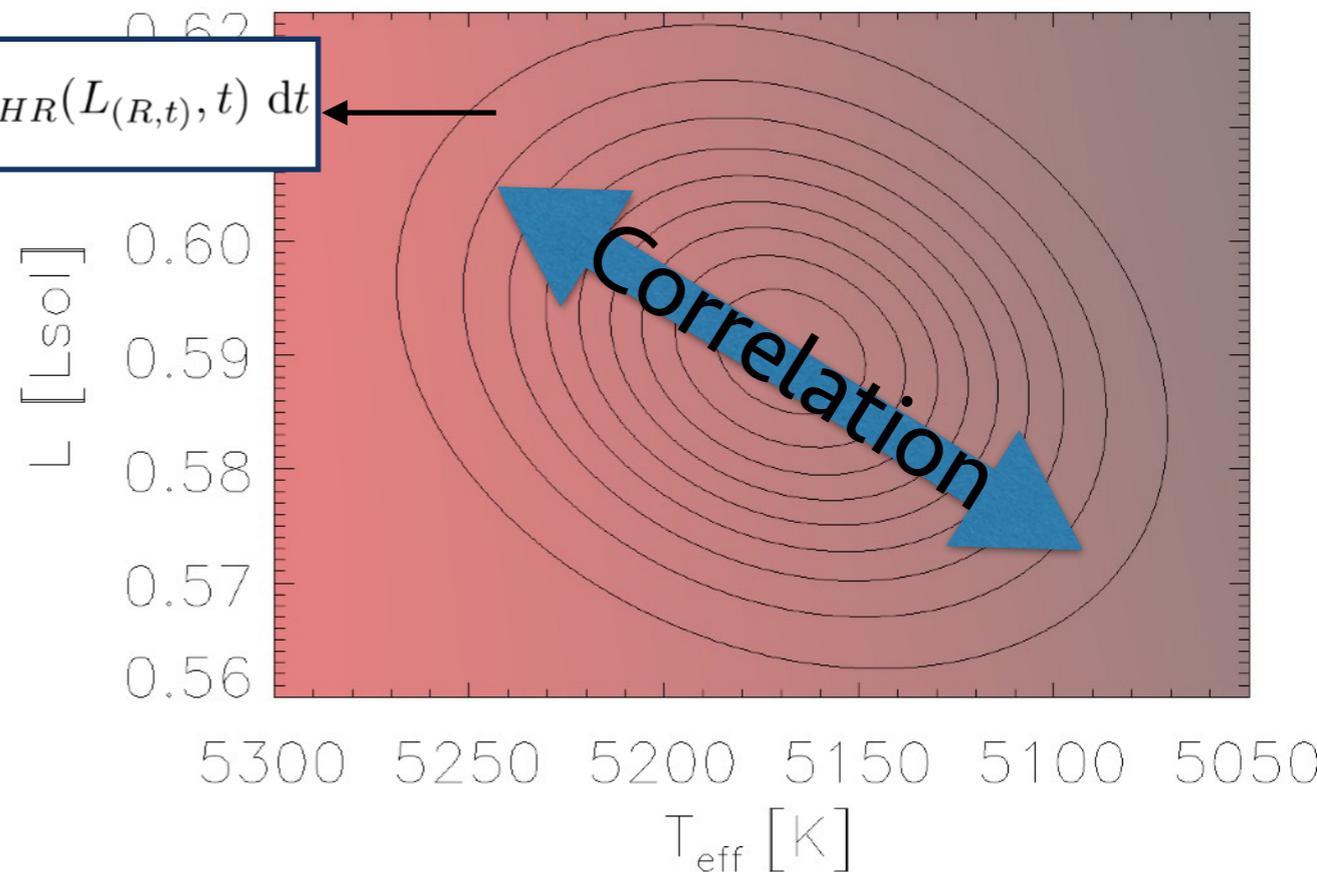
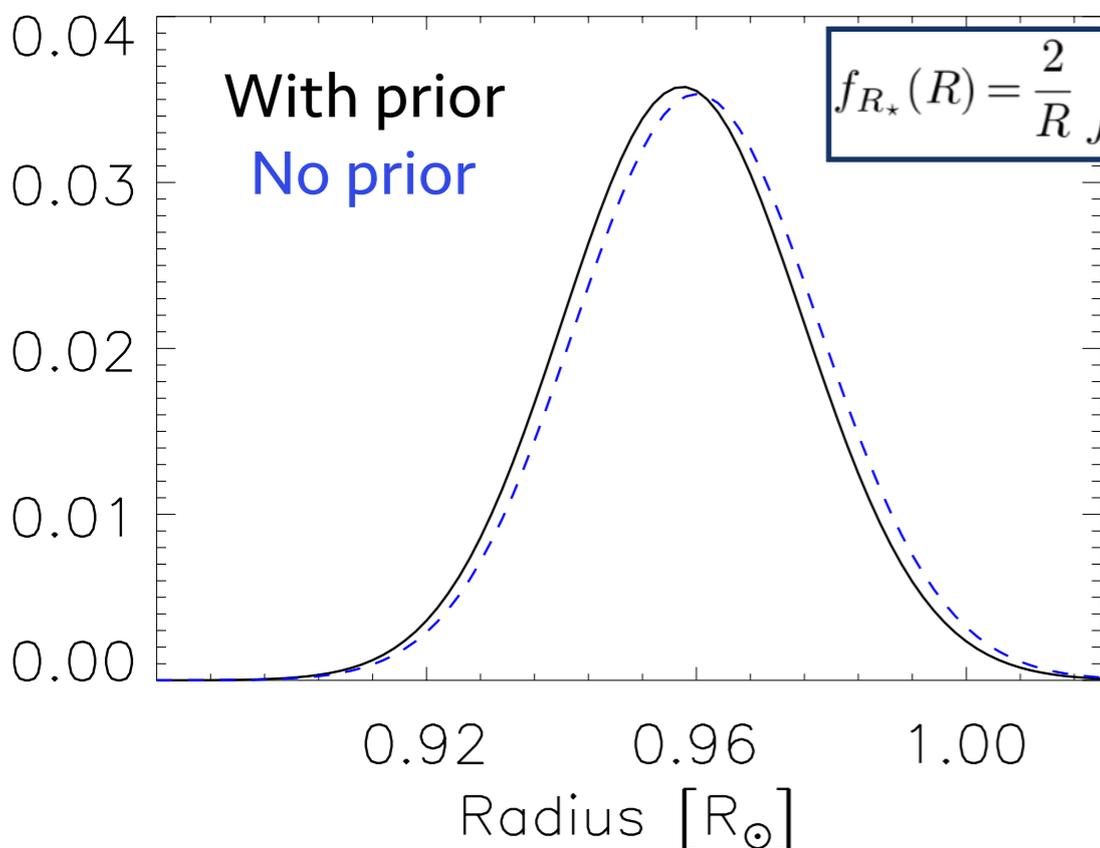
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Interferometry is precise!
The prior does not bring much.

Prior: density of stars in the HR diagram of the Hipparcos sample (color).

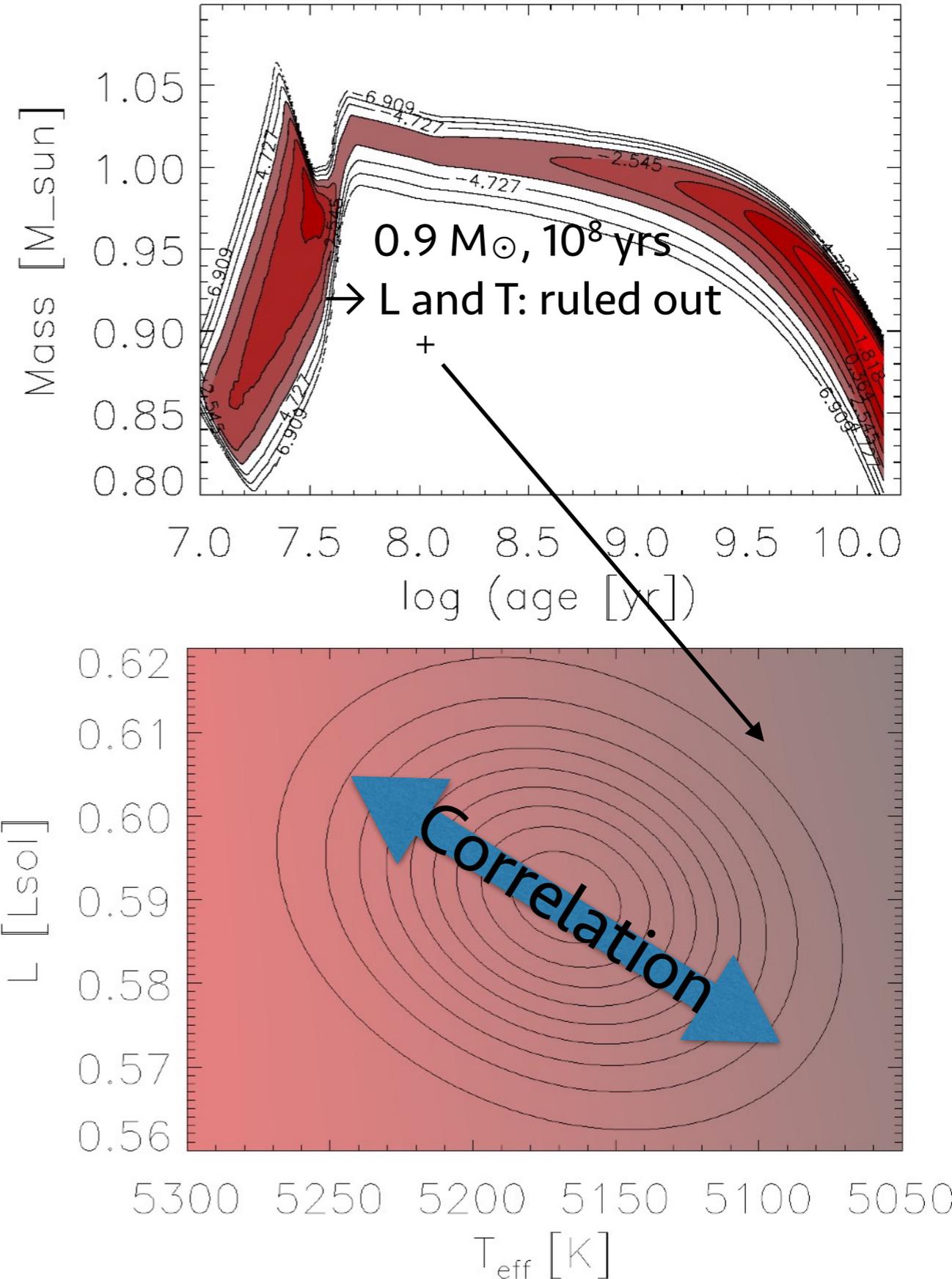
level curves



55 CNC: A BAYESIAN APPROACH

Results:

- Bayesian or not: 2 solutions
- But Lithium detection rules out the old solution! Consistent with young solution (age and mass) of [Ligi et al. \(2016\)](#).
- Still, different parameters in the model → different, inconsistent masses for the young solution: CES2MO ([Lebreton & Goupil 2014](#)) gives M_{\star} from 0.950 ± 0.015 to $0.989 \pm 0.020 M_{\odot}$



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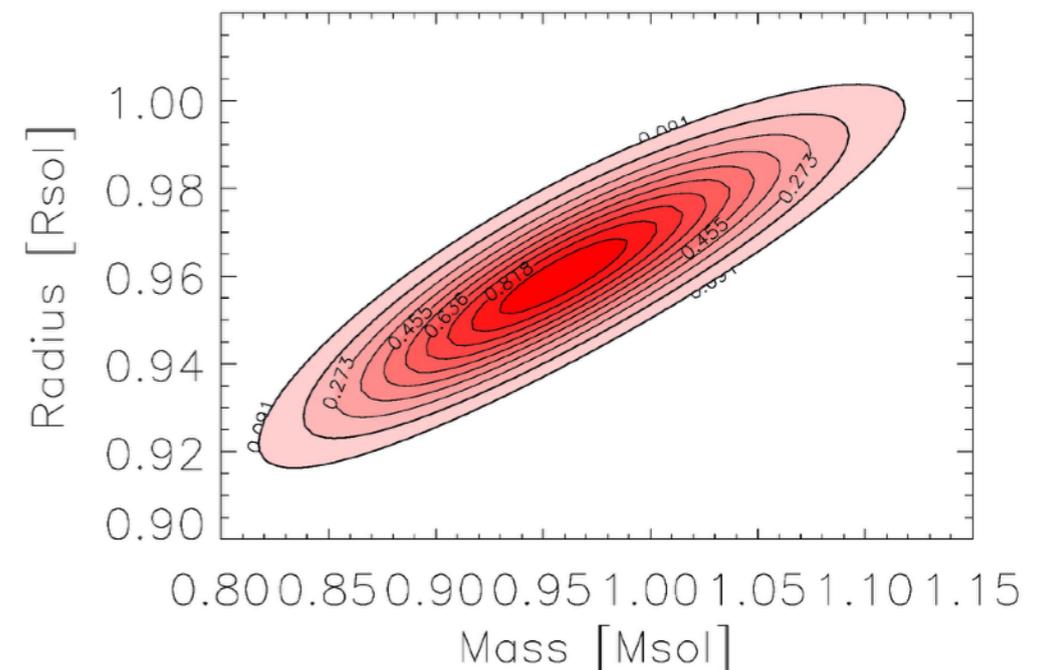
measure of stellar density ρ_{\star} (Maxted et al. 2015, Seager & Mallén-Ornelas 2003)

Measure of R_{\star} by interferometry $\rightarrow M_{\star} = (4\pi/3)R_{\star}^3 \rho_{\star}$ (Ligi et al. 2016)

From the PDF of R_{\star} and ρ_{\star} ,
analytic joint likelihood of $M_{\star} - R_{\star}$.

$$\mathcal{L}_{MR_{\star}}(M, R) = \frac{3}{4\pi R^3} \times f_{R_{\star}}(R) \times f_{\rho_{\star}}\left(\frac{3M}{4\pi R^3}\right)$$

- \rightarrow Strong correlation (0.85)!
- \rightarrow Different M_{\star} than von Braun et al. (2011) based on isochrones.



USING STELLAR DENSITY AND ANGULAR DIAMETERS

Transit duration: $T = 2R_{\star} / a\Omega$

Period: $P = 2\pi / \Omega$



$$P/T^3 = (\pi^2 G/3) \rho_{\star}$$

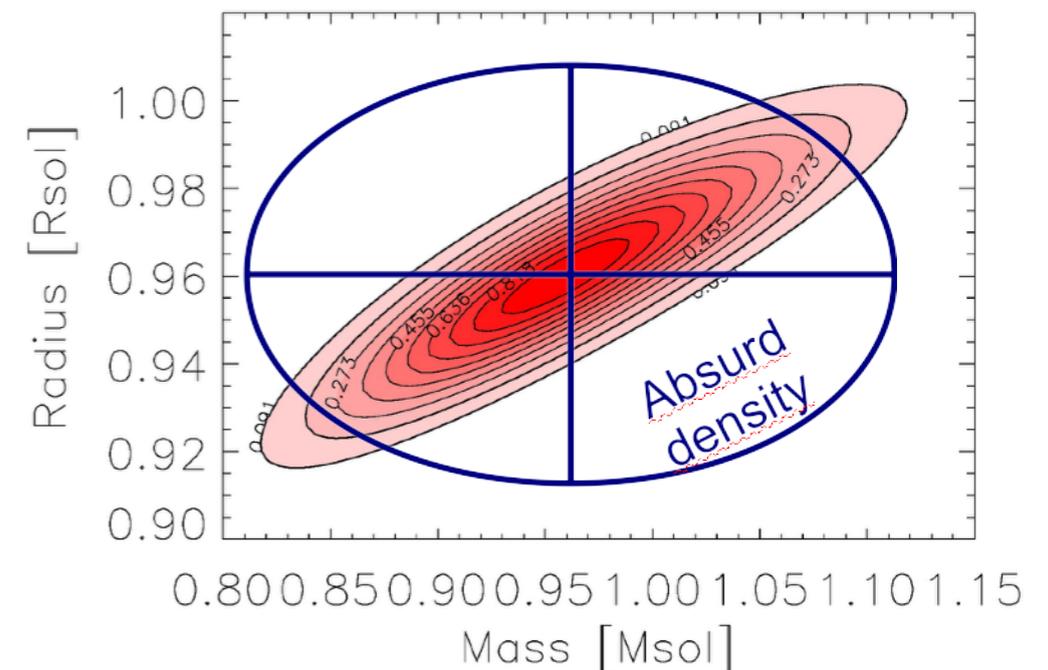
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Taking the values of R_{\star} and M_{\star} from Ligi et al. (2016), one gets the large, wrong blue ellipse.



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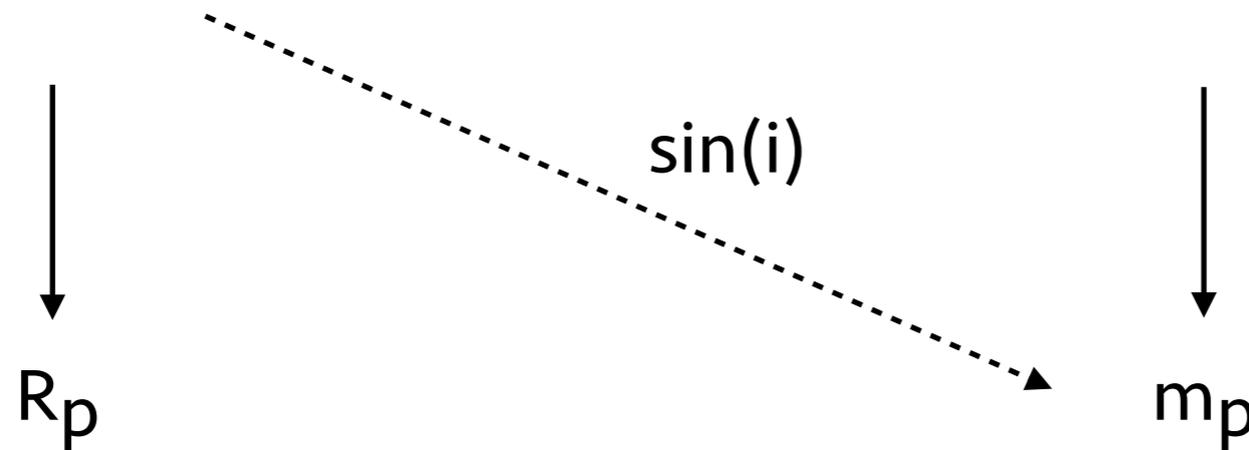
Measure of R_{\star} by interferometry $\rightarrow M_{\star} = (4\pi/3) R_{\star}^3 \rho_{\star}$ (Ligi et al. 2016)

Transit light curve:

$$R_p = R_{\star} \times \sqrt{TD}$$

RV measurements:

$$m_p \sin(i) = M_{\star} K (P/2\pi G M_{\star})^{1/3}$$



Some calculation to decrease the error bar...

$$\rho_p = \frac{3^{1/3}}{2\pi^{2/3} G^{1/3}} \rho_{\star}^{2/3} R_{\star}^{-1} T D^{-3/2} P^{1/3} K (1 - e^2)^{1/2}$$

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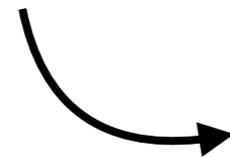
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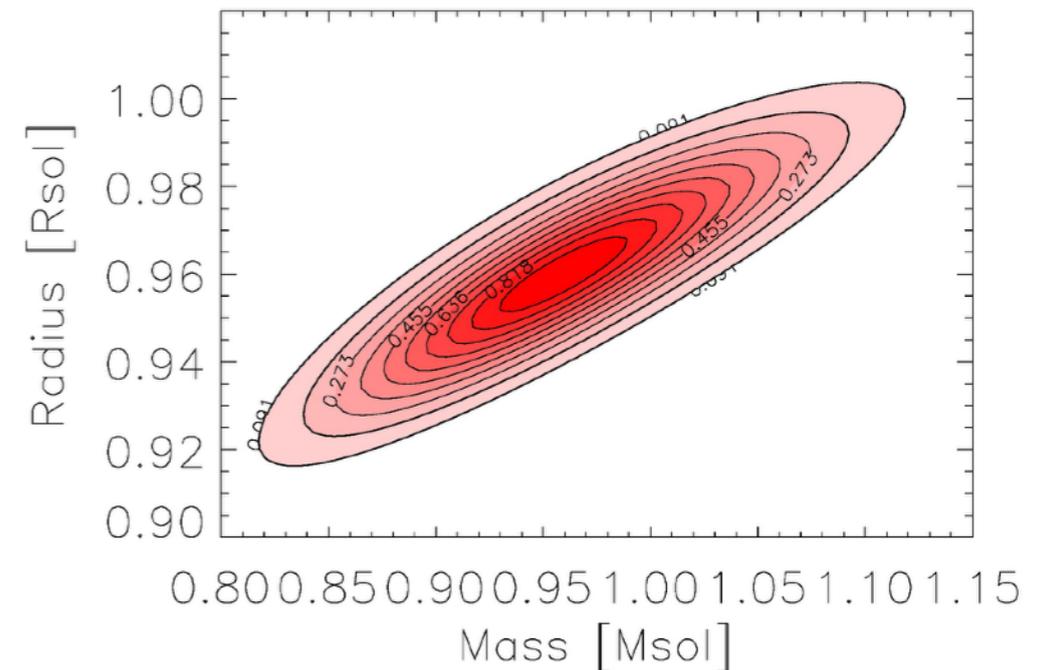
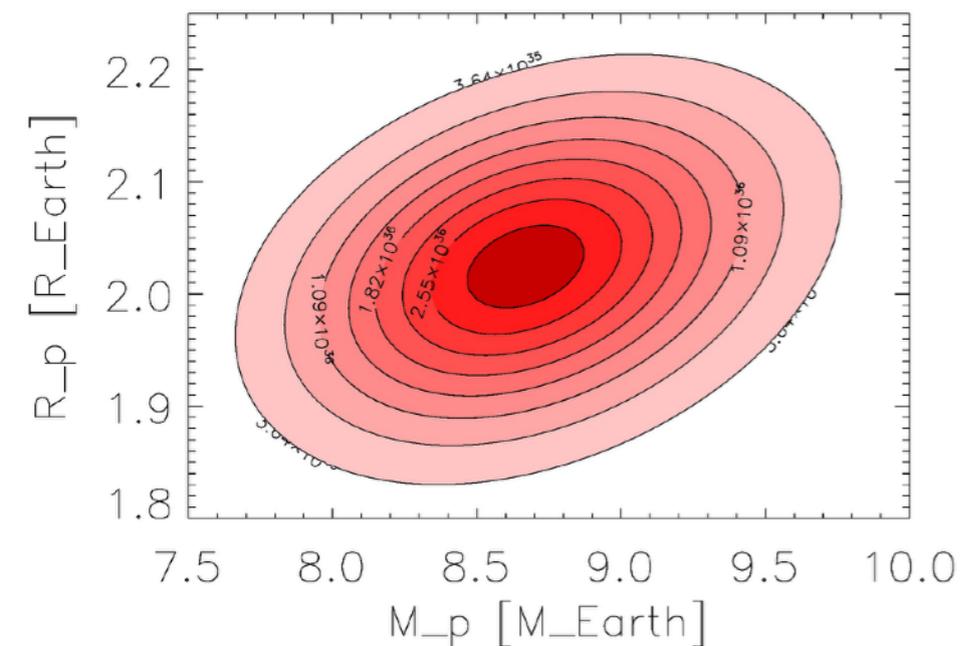
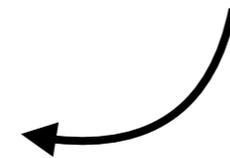
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\rightarrow Analytic PDF of ρ_p
 \rightarrow Joint PDF of $m_p - R_p$



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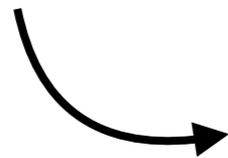
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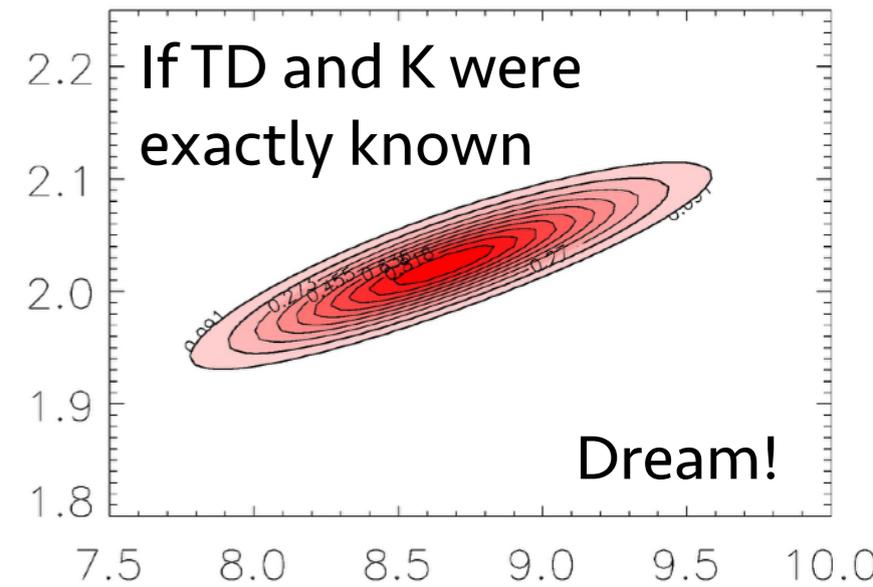
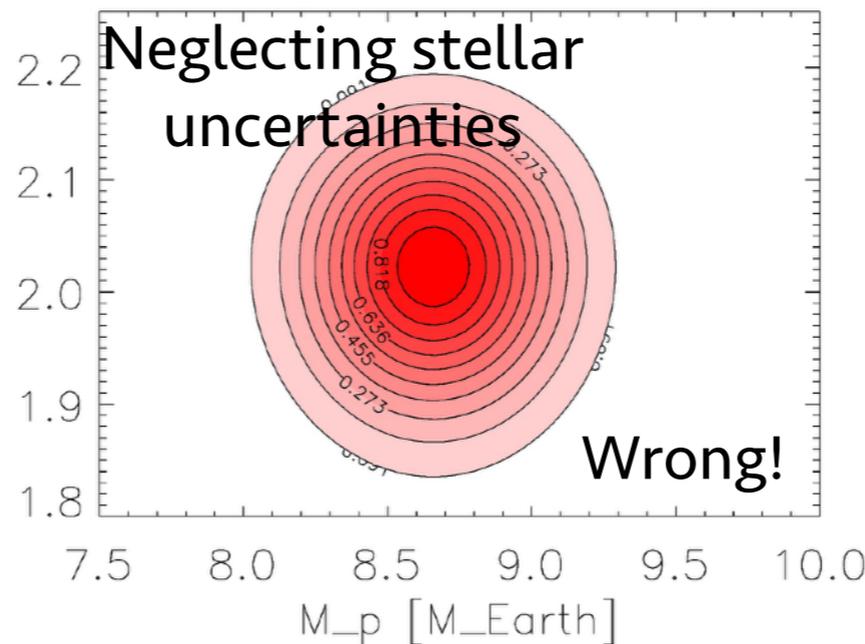
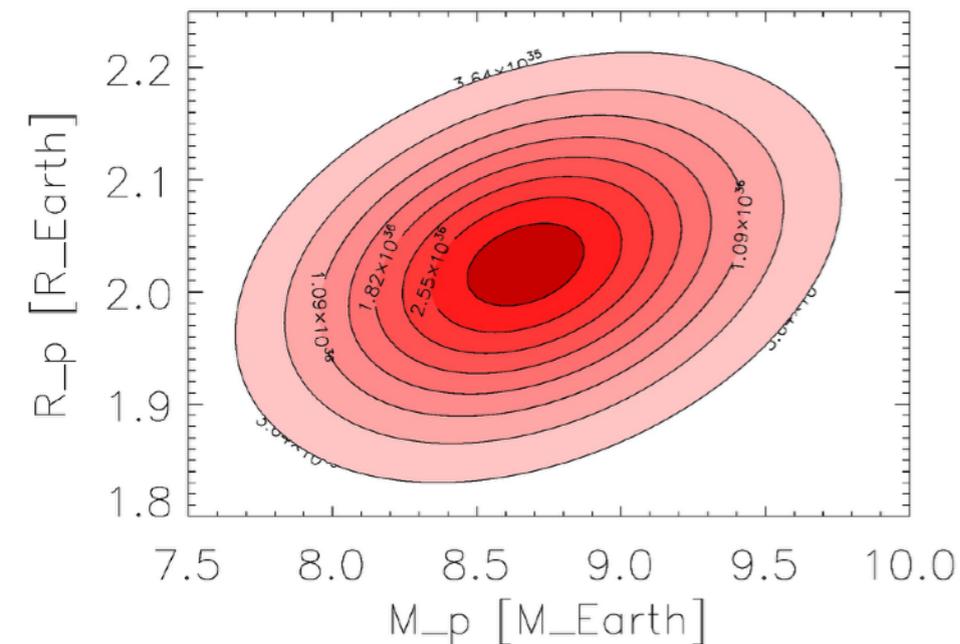
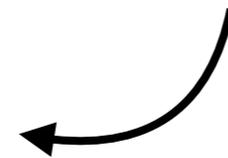
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\rightarrow Analytic PDF of ρ_p

\rightarrow Joint PDF of $m_p - R_p$



55 CNC E: INTERNAL COMPOSITION

Internal structure model developed by [Dorn et al. \(2017\)](#).

Input:

Original data : m_p , R_p (uncorrelated), a , L_\star .

Correlation between m_p and R_p (0.30).

Hypothetical correlation (0.85).

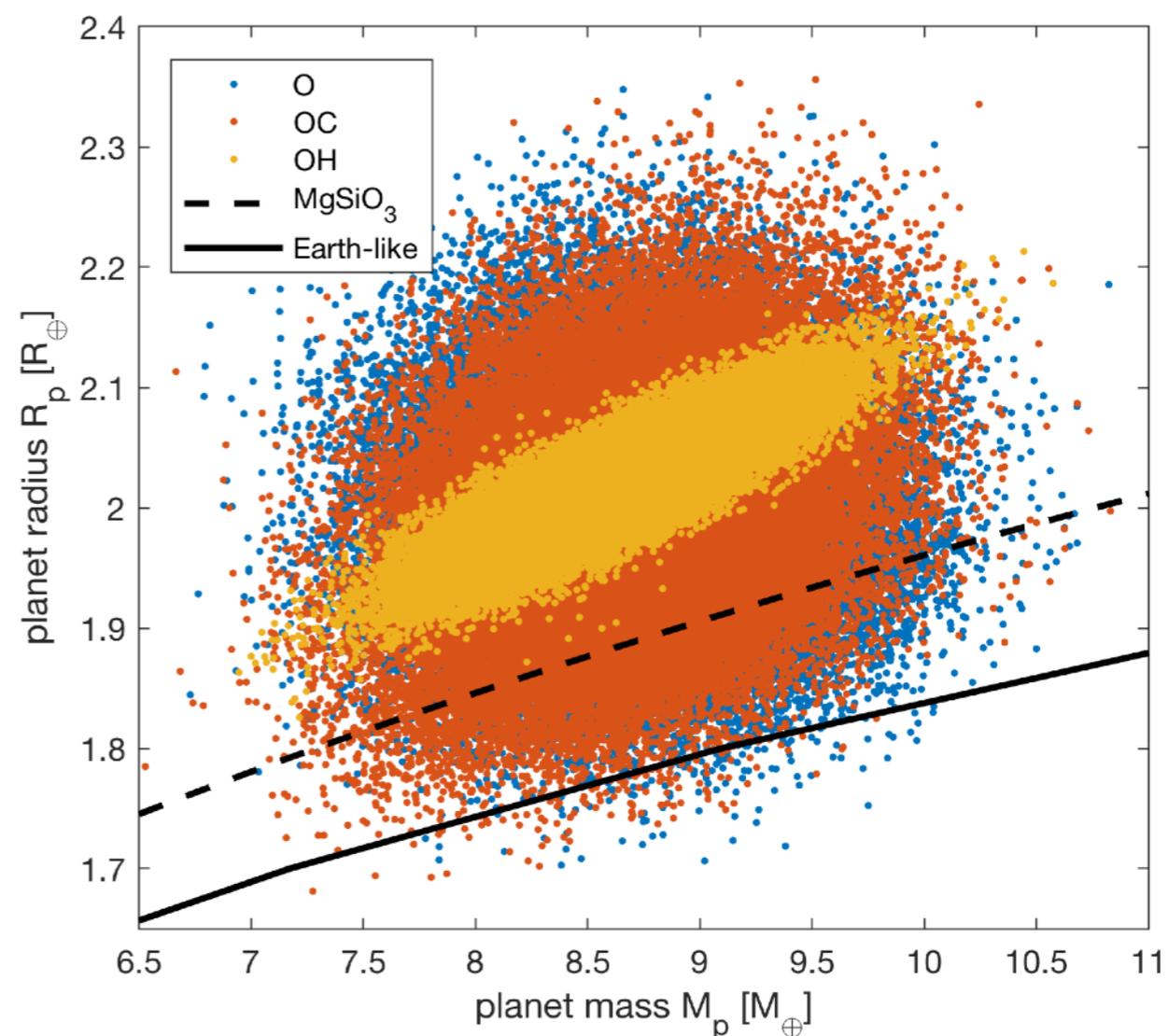
Abundances : stellar Fe/Si, Mg/Si.

Output:

PDF (or CDF) of all the internal parameters.

We test the importance of the various data

O, C, H, A.



55 CNC E: INTERNAL COMPOSITION

Input :

Original data m_p, \dots

Correl. m_p-R_p (0.30)

Hypothetical corr. (0.85)

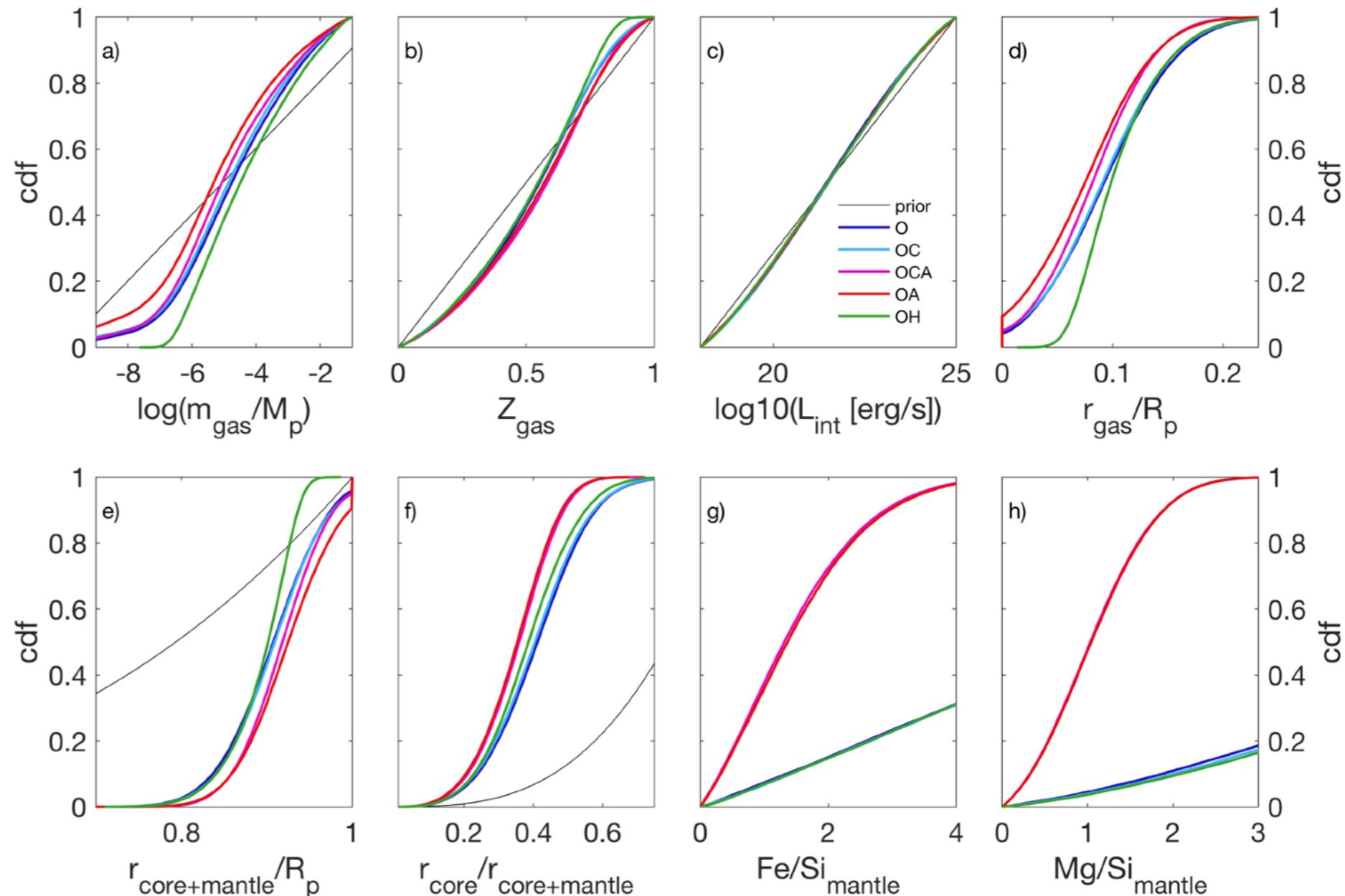
Abundances

Results :

A \rightarrow composition of the mantle

C \rightarrow gas layer

H \rightarrow could rule out pure solid composition



OCA case: our best constrains on all the parameters.

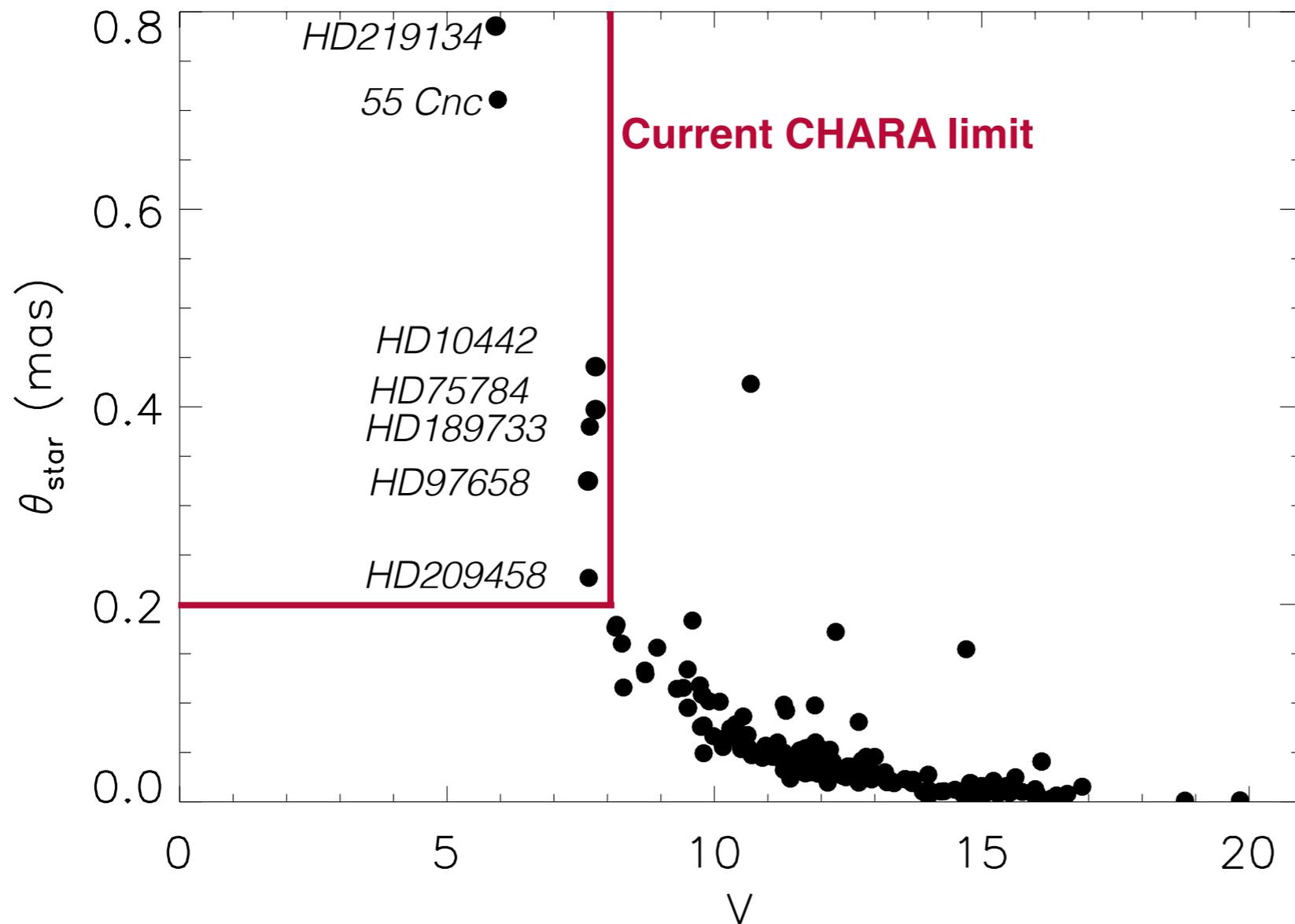
INTERFEROMETRY FOR FAINTER STARS

Combining interferometry with other methods, we:

- reduced the uncertainties on the parameters of 55 Cnc, using direct measurements and an analytical approach,
 - reduced the possible range of internal structures of 55 Cnc e using correlations and abundances.
- Is it possible to perform a similar analysis with other systems?

INTERFEROMETRY FOR FAINTER STARS

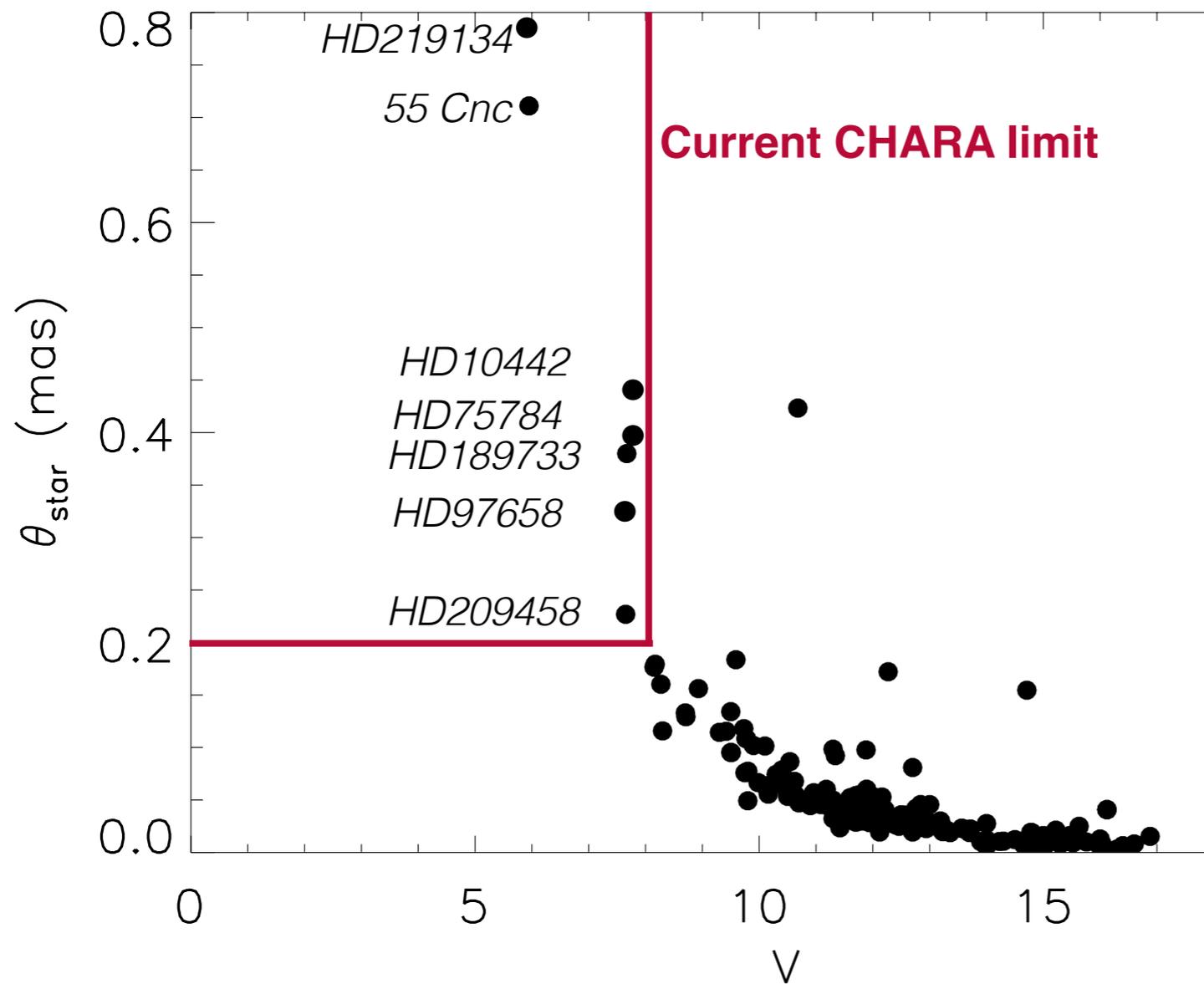
Stars harbouring transiting exoplanets



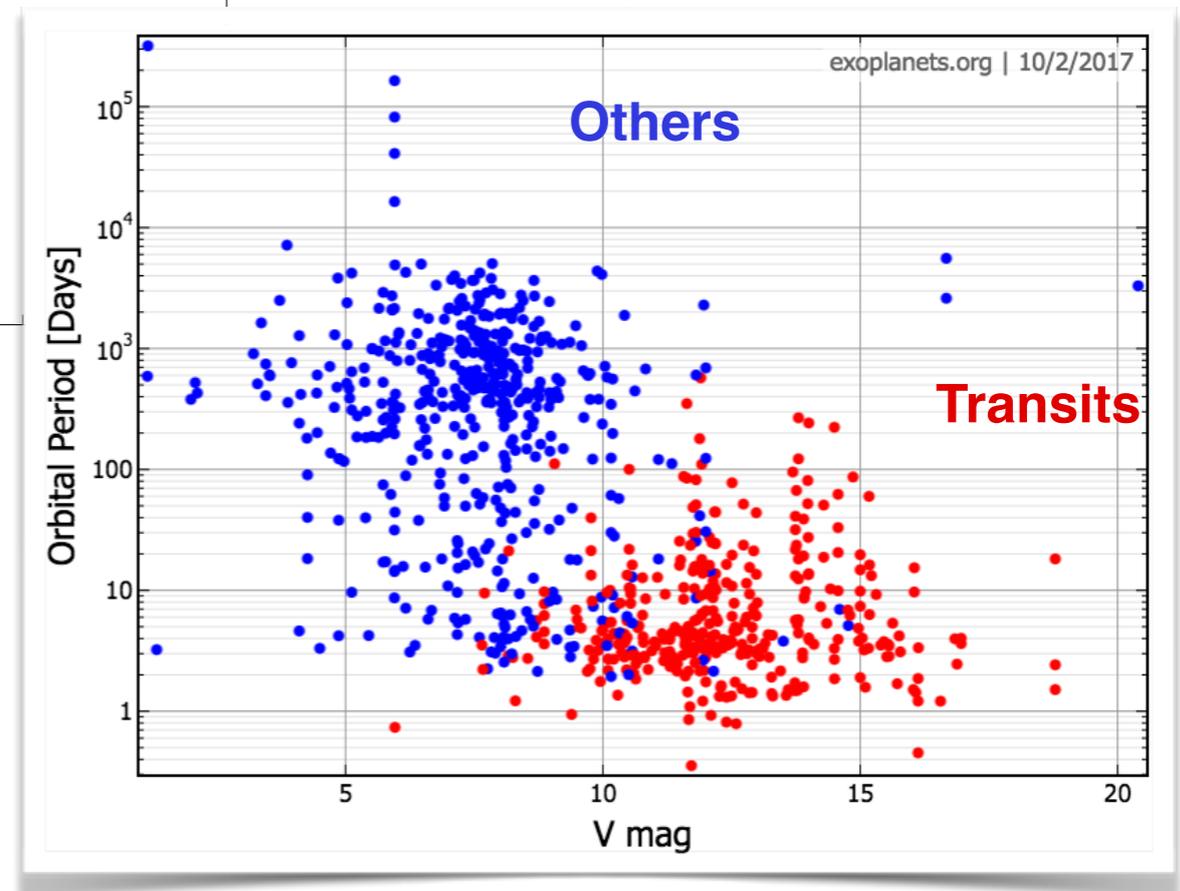
- Few systems are currently accessible with interferometers

INTERFEROMETRY FOR FAINTER STARS

Stars harbouring transiting exoplanets

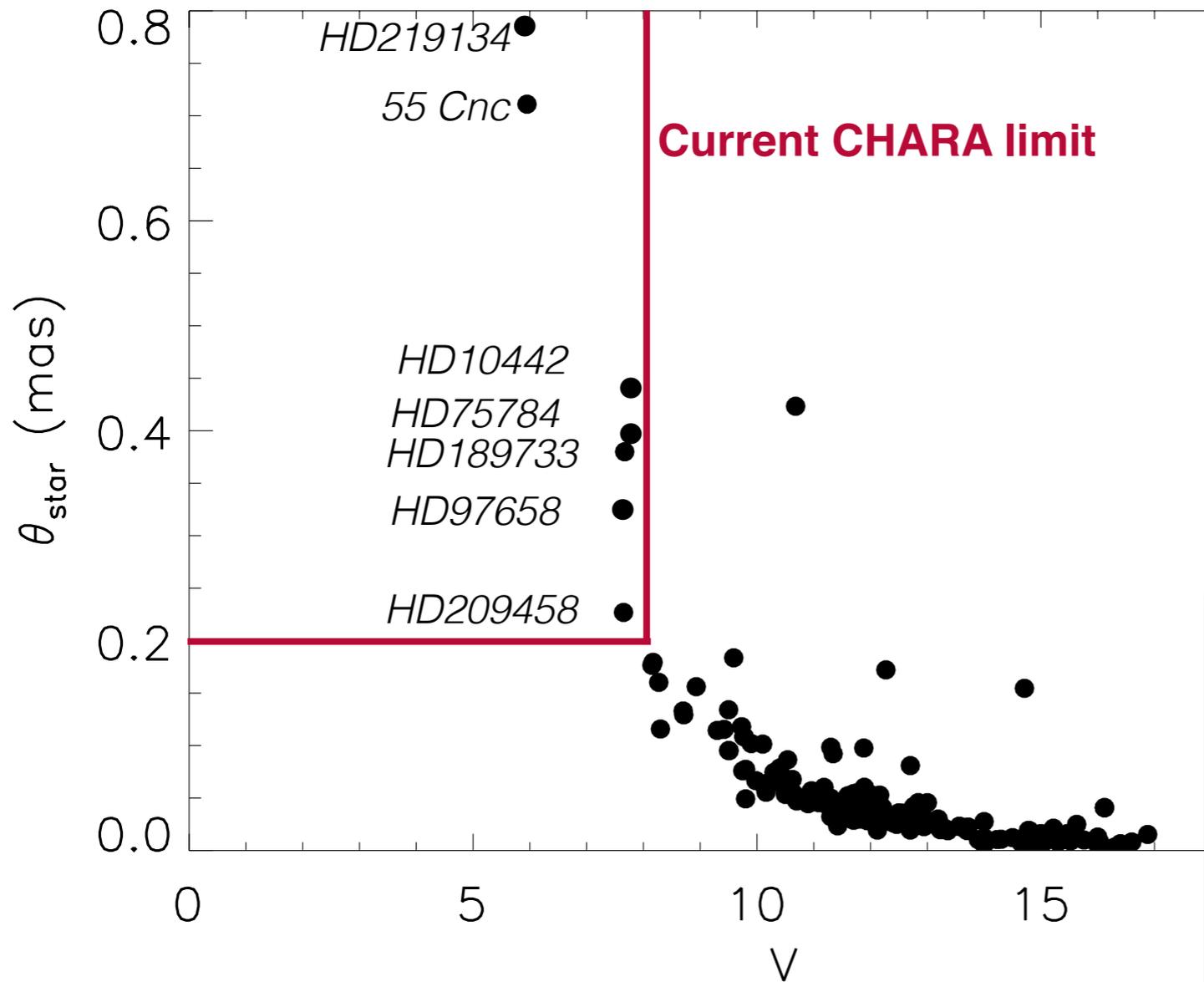


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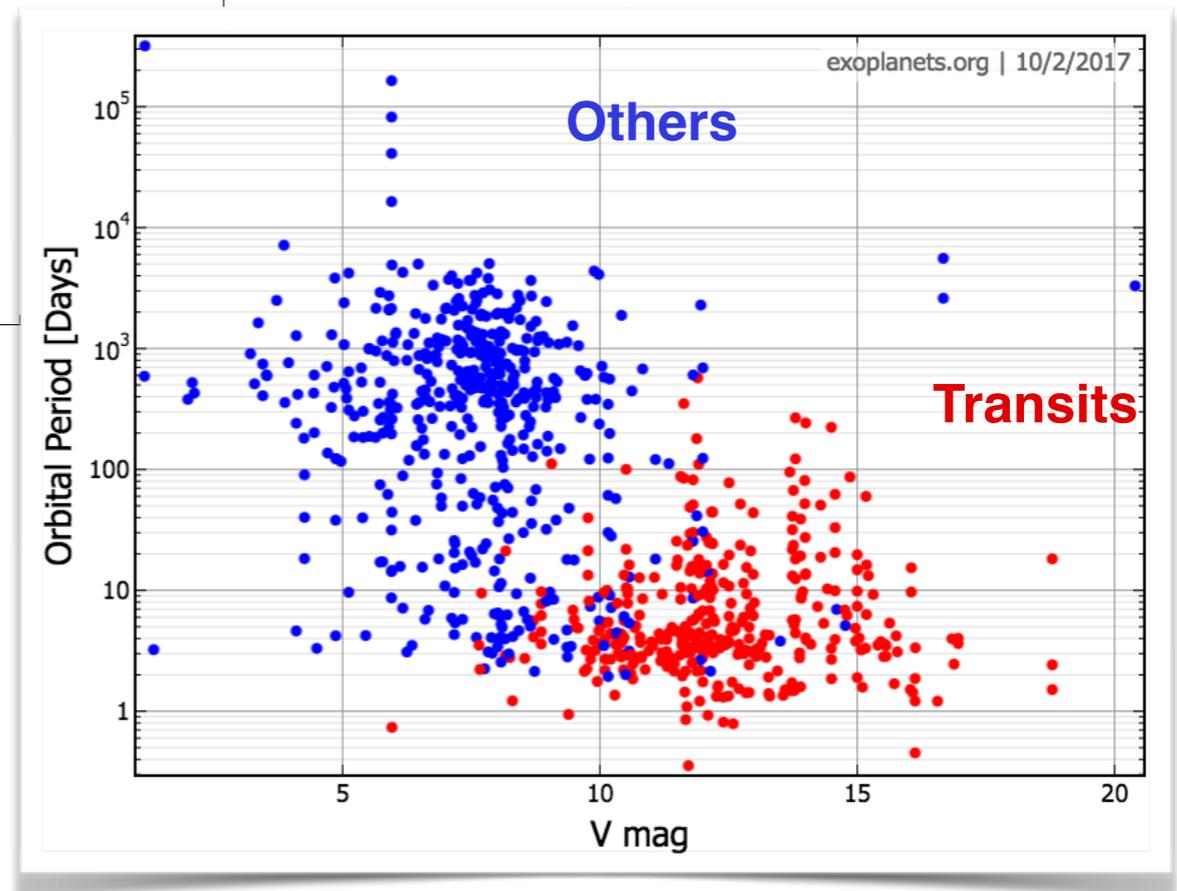
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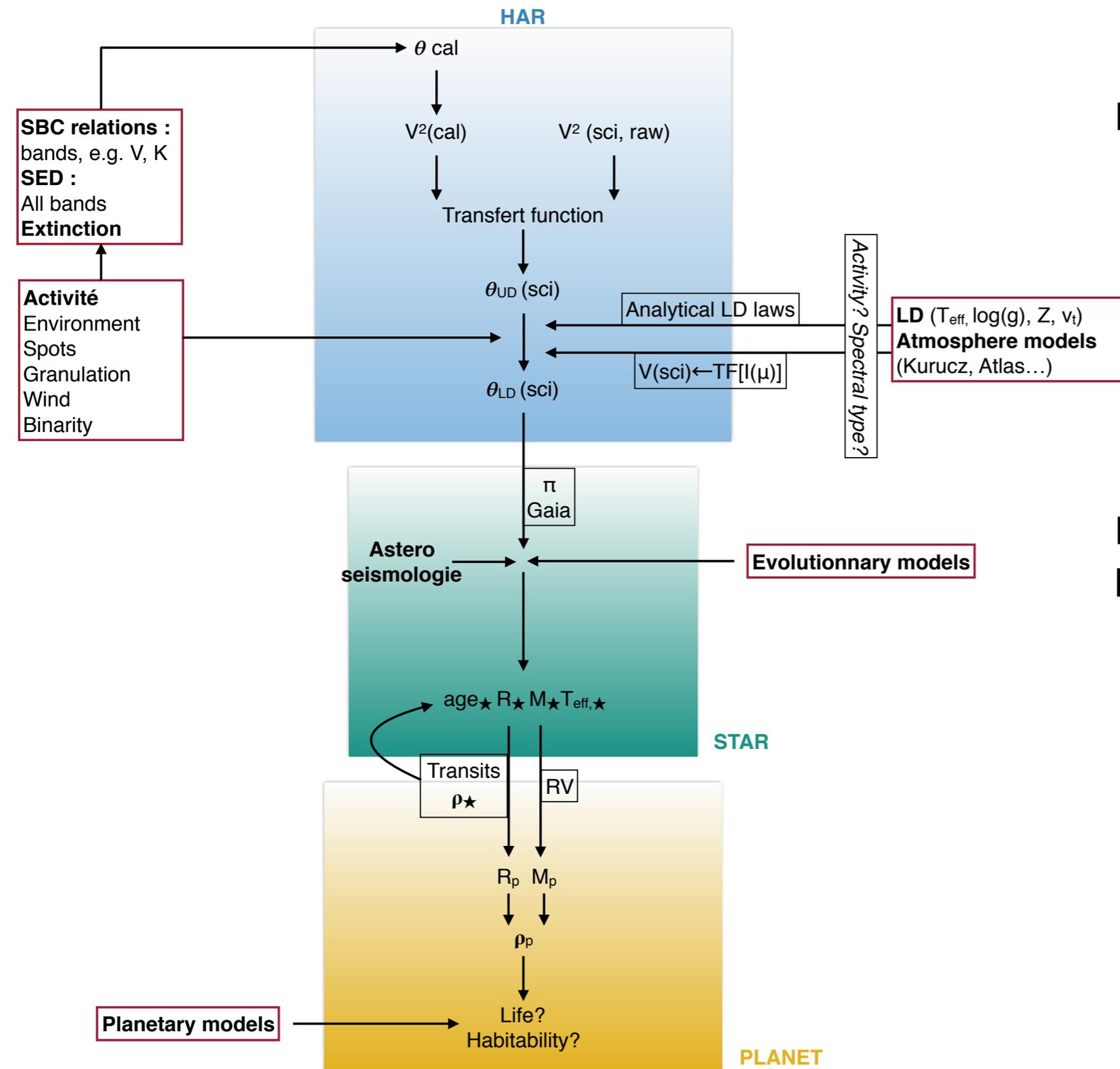


- Few systems are currently accessible with interferometers
- This will change soon with the development of future facilities (see talk of L. Bigot)
- Still, some stars will be too faint.

→ The SPICA project



THE SPICA PROJECT: PROBLEMATICS



Bias on diameters

- limb-darkening
- rotation
- pulsation
- circumstellaire environment
- activity

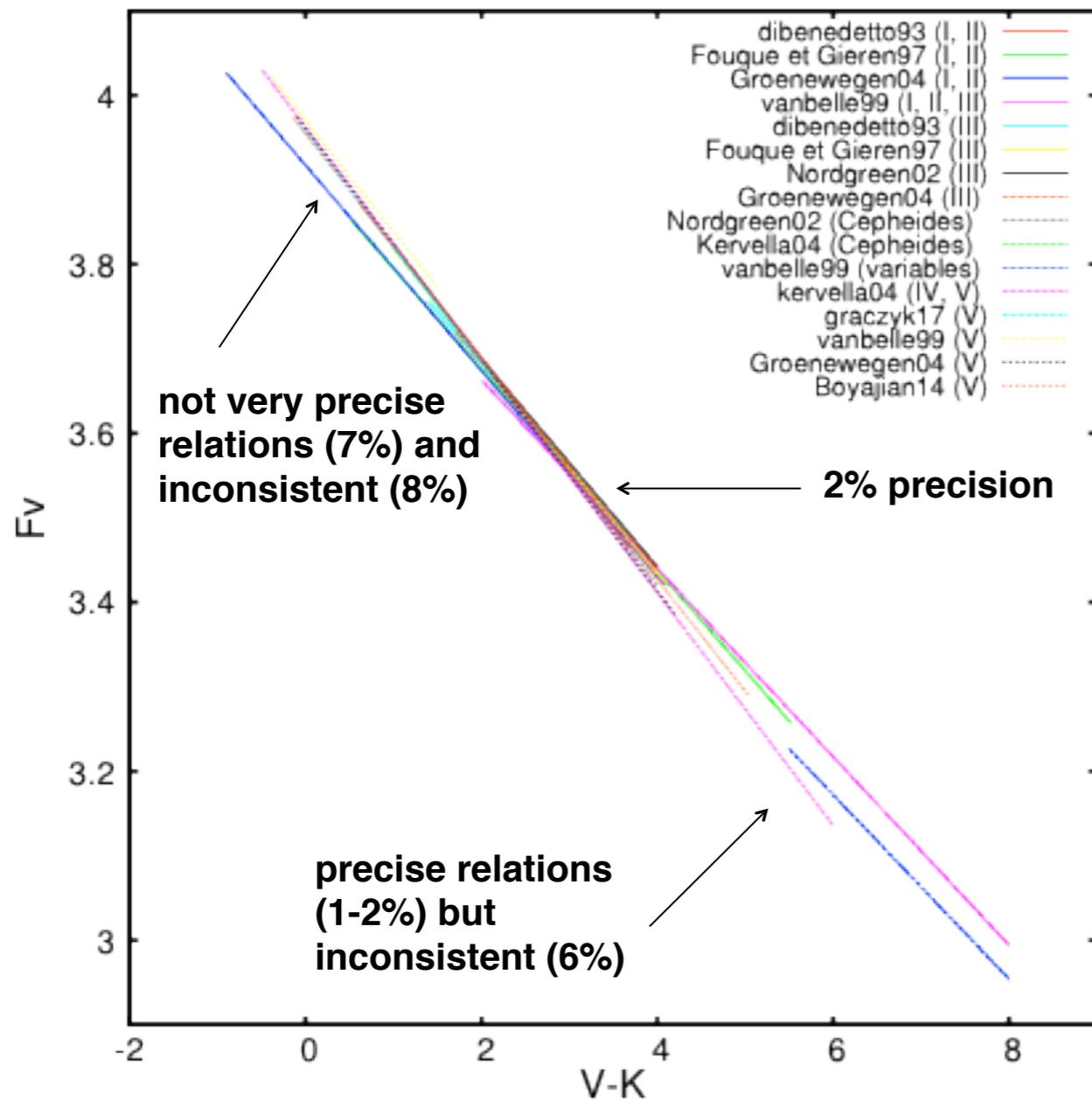
But need for an accurate and precise estimation

- to improve surface brightness-color (SBC) relations,
- to have reliable measurements of stellar diameters and stellar parameters
- SED fitting

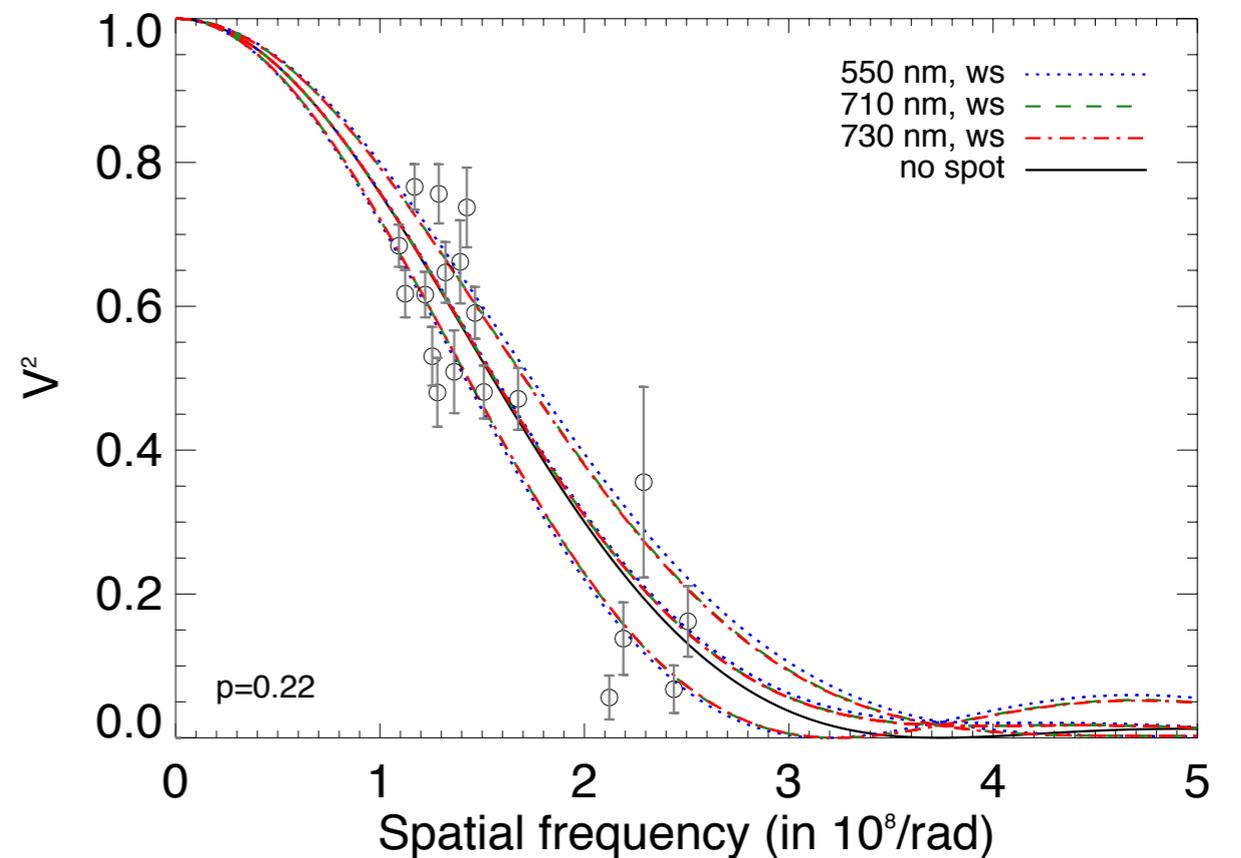
(See talk of L. Bigot)

THE SPICA PROJECT: PROBLEMATICS

Examples of SBC relations



GJ504: the age determines the nature of the detected companion

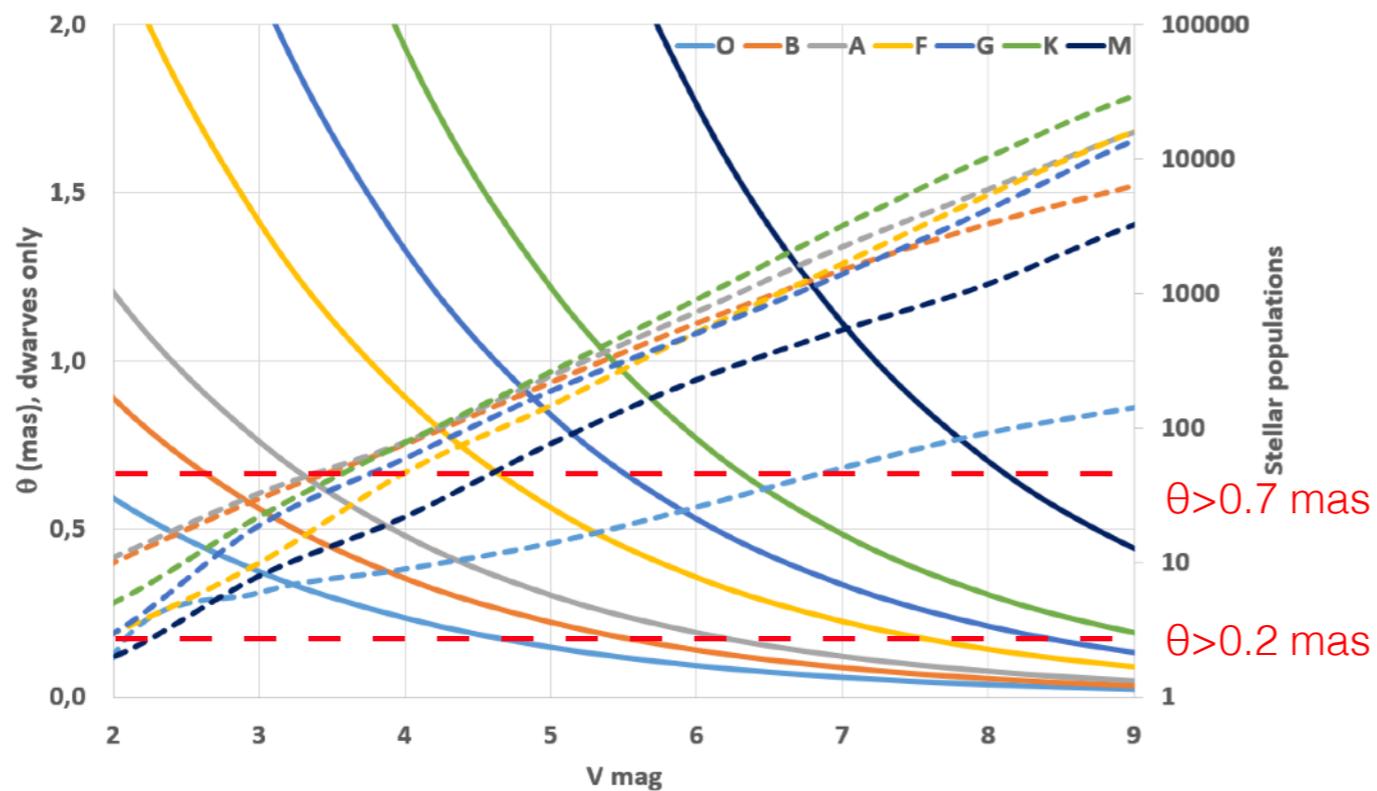


GJ504, Bonnefoy et al., accepted, using COMETS code (Ligi et al. 2015)

Effects of spots on the visibility curve could change the diameter.

THE SPICA PROJECT: GOAL

Diameters and stellar populations of CHARA

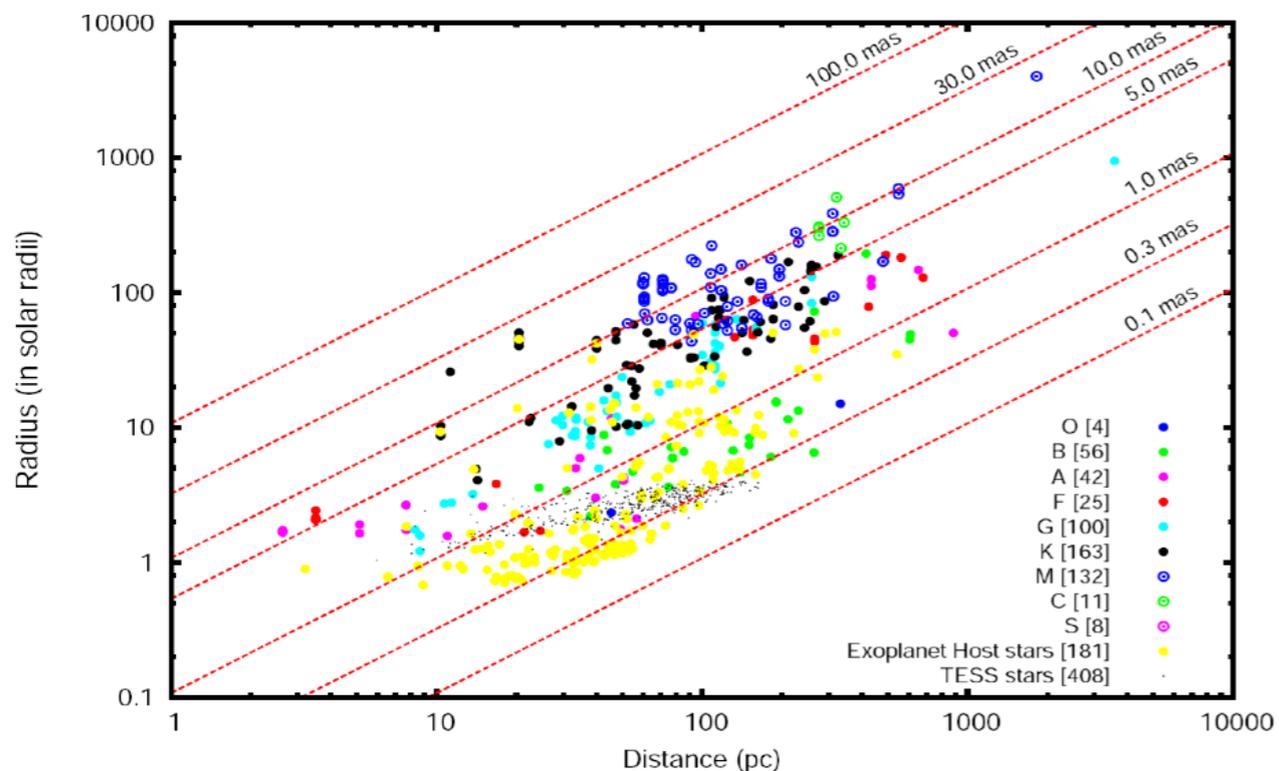


A large program for:

- interferometric measurements of angular diameters of stars compatible with PLATO/TESS/CHEOPS → **bright stars** (mag ~8, then 9)
- improving SBC relations → **faint stars**
- imaging stellar surfaces → **effects of activity, rotations...**

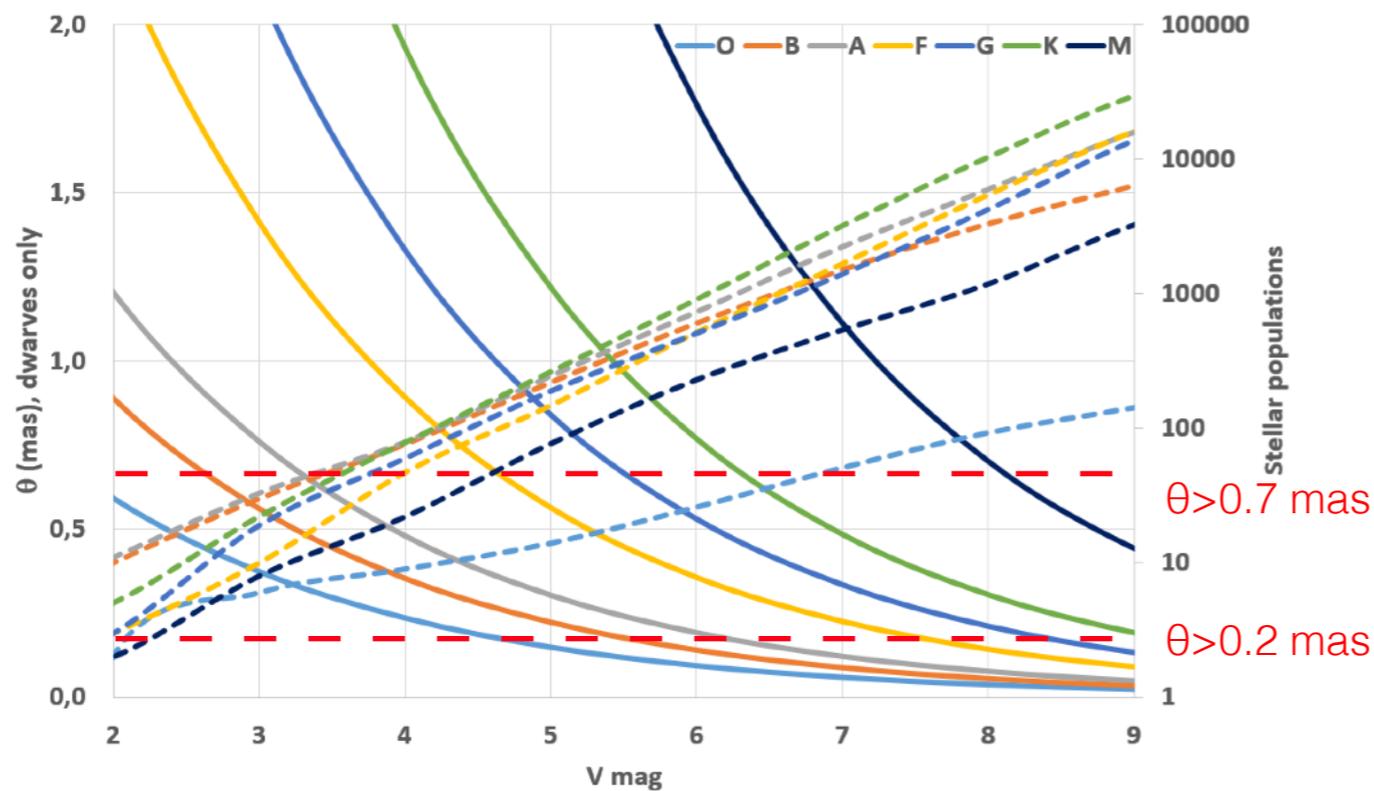
Requirements:

- Coverage of class I-V and spectral types OBAF + K-IV/V et M-IV/V
- Host stars and seismic stars
- Expected to measure the limb-darkening
- Taking into account stellar activity
- Precision of ~1% on diameters and SBC relations



THE SPICA PROJECT: GOAL

Diameters and stellar populations of CHARA

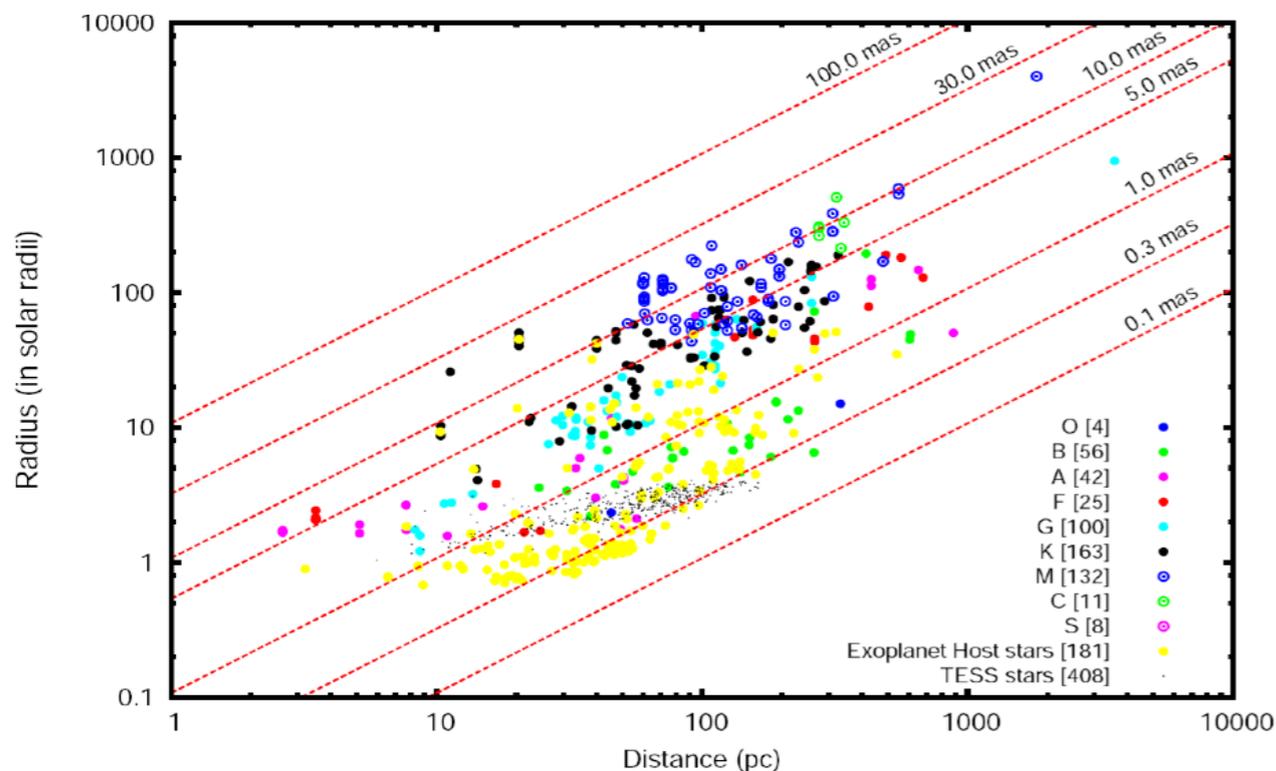


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Use of AO recently installed on CHARA
+
6 telescopes at the same time

THE SPICA PROJECT: CONCLUSION

Interferometry is complementary to PLATO data:

- Asteroseismology cannot be applied to every stellar types
 - Ex: not possible for sp. types K → M
- Stellar models: difficulties for some stellar types (see talks of yesterday)
 - Ex: M stars

Interferometry can be applied to all type of stars, given that:

- they are bright (direct measurements; PLATO/TESS/CHEOPS targets)
- we have a good photometry (SBC relations)

Most direct technique for the measurement of stellar diameters.

→ Expected to follow-up many PLATO targets.

INTERFEROMETRY & EXOPLANETS

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Milazzo, Sicily · 22-25 May 2018

THANK YOU FOR YOUR
ATTENTION